

What You Will Learn

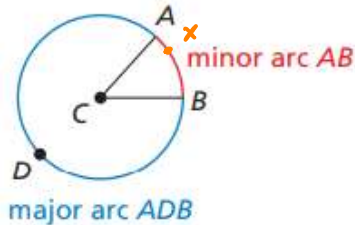
- Find arc measures.

Finding Arc Measures

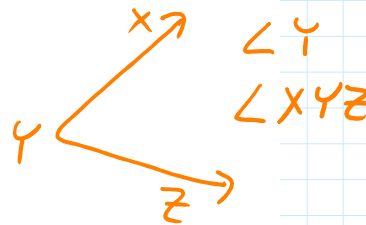
A **central angle** of a circle is an angle whose vertex is the center of the circle. In the diagram, $\angle ACB$ is a central angle of $\odot C$.

If $m\angle ACB$ is less than 180° , then the points on $\odot C$ that lie in the interior of $\angle ACB$ form a **minor arc** with endpoints A and B . The points on $\odot C$ that do not lie on the minor arc AB form a **major arc** with endpoints A and B . A **semicircle** is an arc with endpoints that are the endpoints of a diameter.

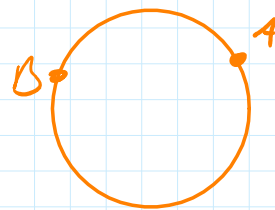
$$\widehat{AB} \neq \overline{AB}$$



$$\widehat{AB} \cong \widehat{AXB}$$



$$m\widehat{AB}$$

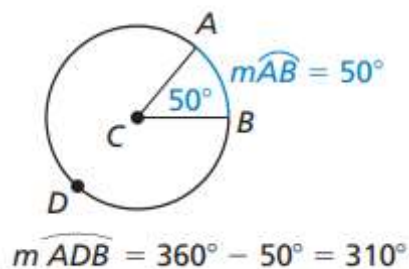


Minor arcs are named by their endpoints. The minor arc associated with $\angle ACB$ is named \widehat{AB} . Major arcs and semicircles are named by their endpoints and a point on the arc. The major arc associated with $\angle ACB$ can be named \widehat{ADB} .

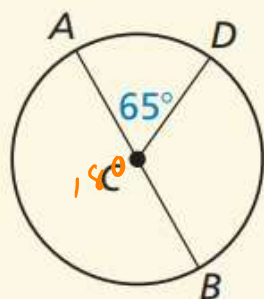
Measuring Arcs

The **measure of a minor arc** is the measure of its central angle. The expression $m\widehat{AB}$ is read as "the measure of arc AB ."

The measure of the entire circle is 360° . The **measure of a major arc** is the difference of 360° and the measure of the related minor arc. The measure of a semicircle is 180° .



Find the measure of each arc of $\odot C$, where \overline{AB} is a diameter.



- \widehat{AD}
- \widehat{DAB}
- \widehat{BDA}

$$m\widehat{AD} = 65^\circ$$

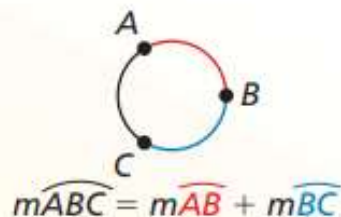
$$m\widehat{DAB} = 245^\circ$$

$$m\widehat{BDA} = 180^\circ$$

$$\begin{array}{r} 180 \\ + 65 \\ \hline 245 \end{array}$$

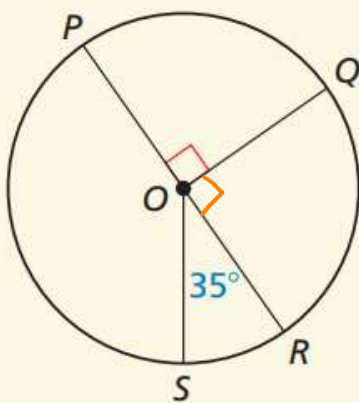
Postulate 10.1 Arc Addition Postulate

The measure of an arc formed by two adjacent arcs is the sum of the measures of the two arcs.



Same ideas as Ruler Addition Postulate
 Angle Addition Postulate

Find the measure of each arc.



- a. \widehat{SQ}
- b. \widehat{RPQ}
- c. \widehat{PRS}

$$m \widehat{SQ} = 125^\circ$$

$$m \widehat{RPQ} = 270^\circ$$

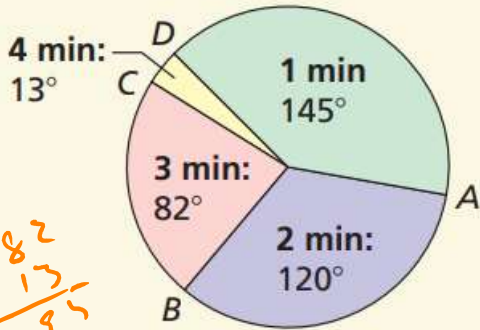
$$m \widehat{PRS} = 215^\circ$$

$$\begin{array}{r} 360 \\ - 90 \\ \hline 270 \end{array} \quad \begin{array}{r} 180 \\ + 90 \\ \hline 270 \end{array}$$

$$90 + 90 + 35 = 215$$

A survey asked people how many minutes they spend brushing their teeth each morning. The circle graph shows the results. Find the indicated arc measures.

For How Long Did You Brush Your Teeth?



Handwritten calculations on the left side of the graph:

$$\begin{array}{r} 360 \\ - 120 \\ \hline 240 \\ - 82 \\ \hline 158 \\ - 13 \\ \hline 145 \end{array}$$

a. $m\widehat{ABC} = 202^\circ$

b. $m\widehat{ACB} = 240^\circ$

c. $m\widehat{BD} = 95^\circ$

d. $m\widehat{CBD} = 347^\circ$

Handwritten calculations on the right side of the graph:

$$\begin{array}{r} 360 \\ - 13 \\ \hline 347 \end{array}$$

Practice *sec* 10.2 pg.
542: 3-17A
